

# **Effect of Particle Size on the Adsorption and Desorption Properties of Oxide Nanoparticles**

***Task 425.023***

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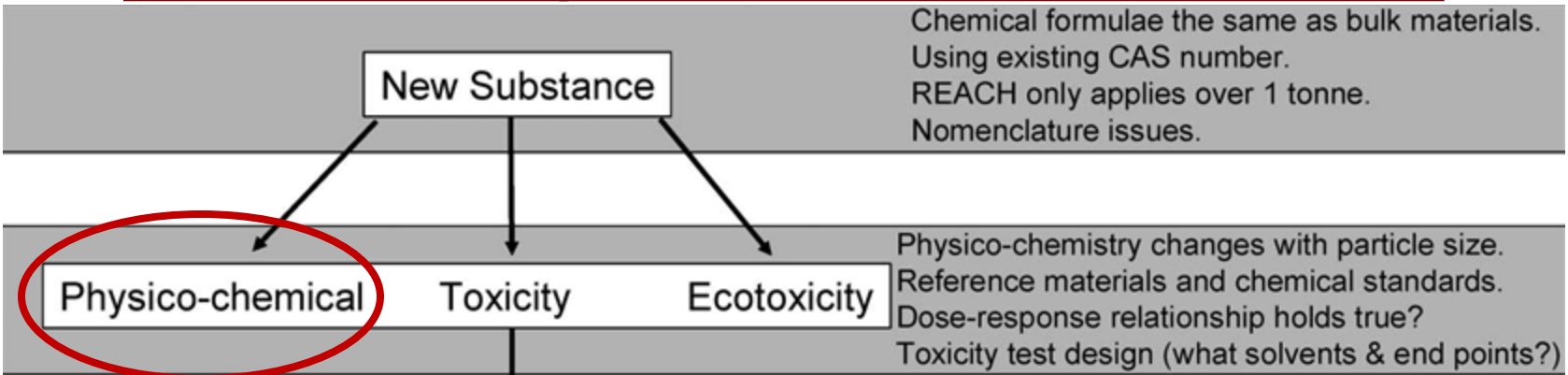
**Dept. Chemical & Environmental Engineering, University of Arizona.**

**Buddy Ratner**

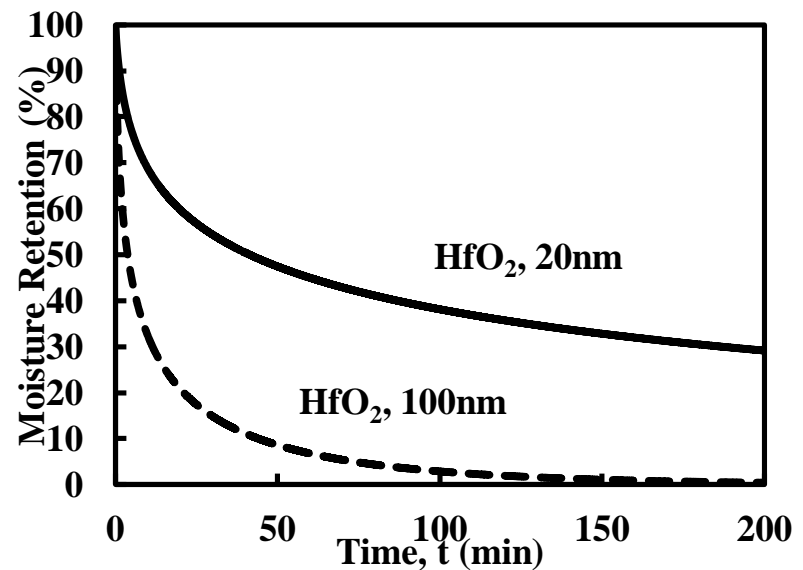
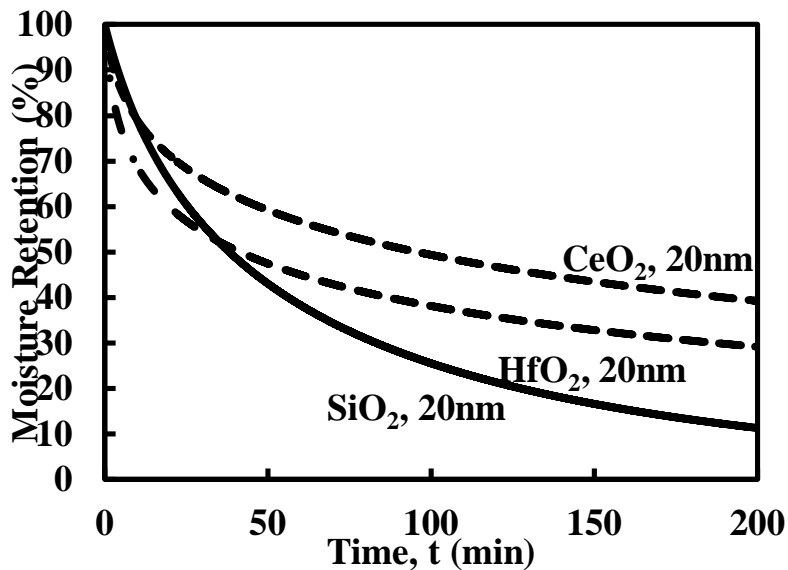
**University of Washington Engineered Biomaterials (UWEB) Center, University of Washington**

***SRC/SEMATECH Engineering Research Center for Environmentally Benign Semiconductor Manufacturing***

# ESH Testing and Evaluation of NPs



## Surface Properties: capacity, affinity, and activation energy



Handy, R.D., Shaw, B.J., 2007. Toxic effects of nanoparticles and nanomaterials: Implications for public health, risk assessment and the public perception of nanotechnology. *Health Risk Society* 9, 125-144.

# Objectives and Method Approach

**Objective:** Characterization of the surface sites on nanoparticles that contribute to concentration, retention, and enhanced transport of toxic chemicals.

**Method approach:** Surface hydroxylation (adsorption and desorption of contaminants).

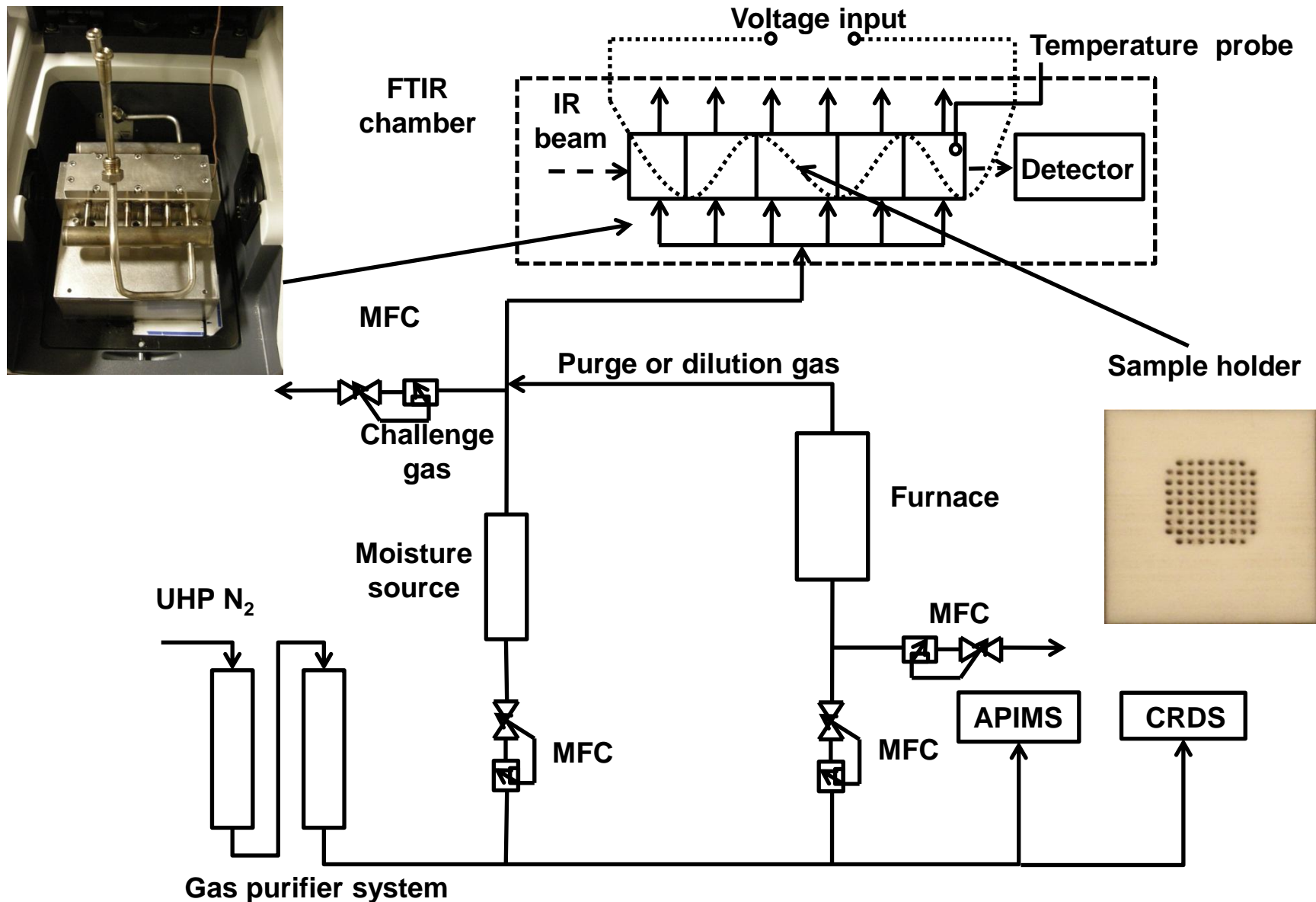
**Materials:** SiO<sub>2</sub>, HfO<sub>2</sub>, and CeO<sub>2</sub>.

**Parameters:** Oxide type, particle size, temperature.

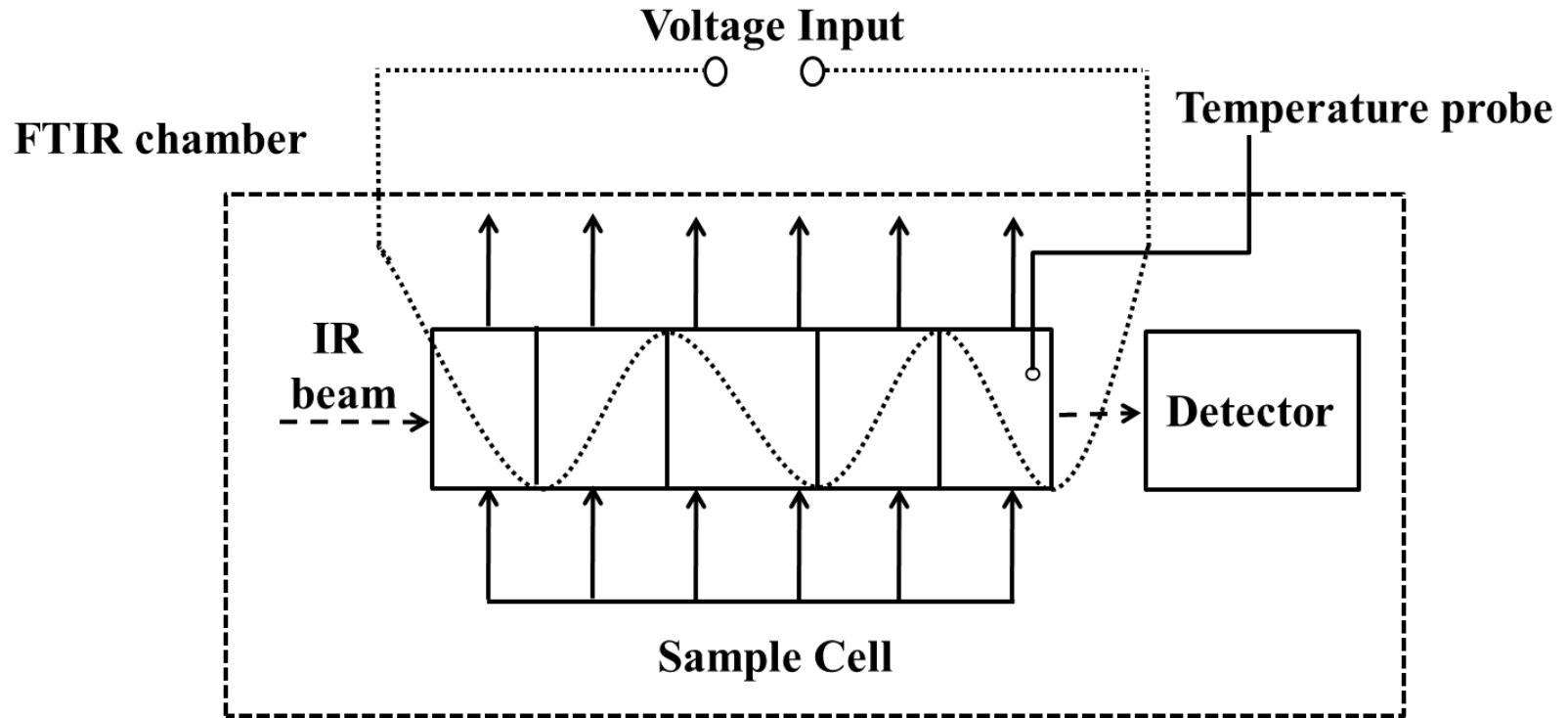
**Results:** Capacity and energetics of capture and retention of contaminants on active sites.

<b>NPs</b>	<b>Supplier</b>	<b>APS* (reported by supplier) (nm)</b>
CeO <sub>2</sub>	Sigma-Aldrich	20 & 50
SiO <sub>2</sub>	Sigma-Aldrich	20
SiO <sub>2</sub>	Nanostructured & Amorphous Materials	80
HfO <sub>2</sub>	Sematech	20
HfO <sub>2</sub>	American Elements	100

# Schematic Diagram of the Experimental Setup



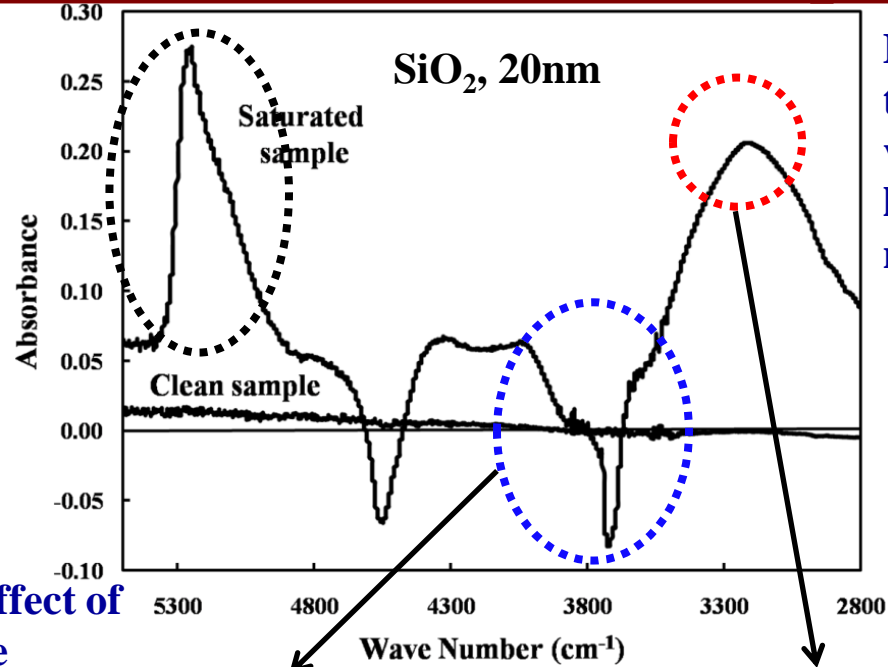
# Heating Element Design



Voltage Input	Temperature
0 V	25°C
30 V	55°C
45 V	80°C
60 V	105°C

# FTIR Spectra of Moisture Adsorption on NPs

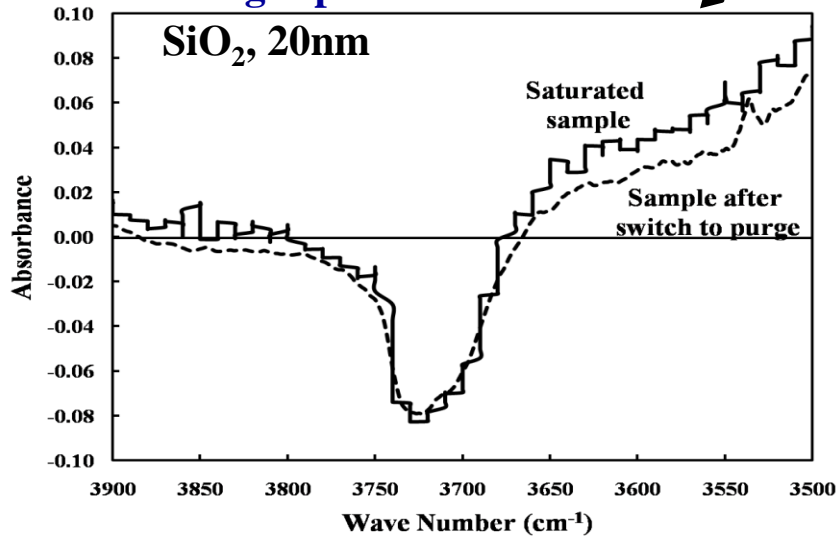
Overtone combination of stretching and bending for water molecules. Wave number:  $5200\text{ cm}^{-1}$



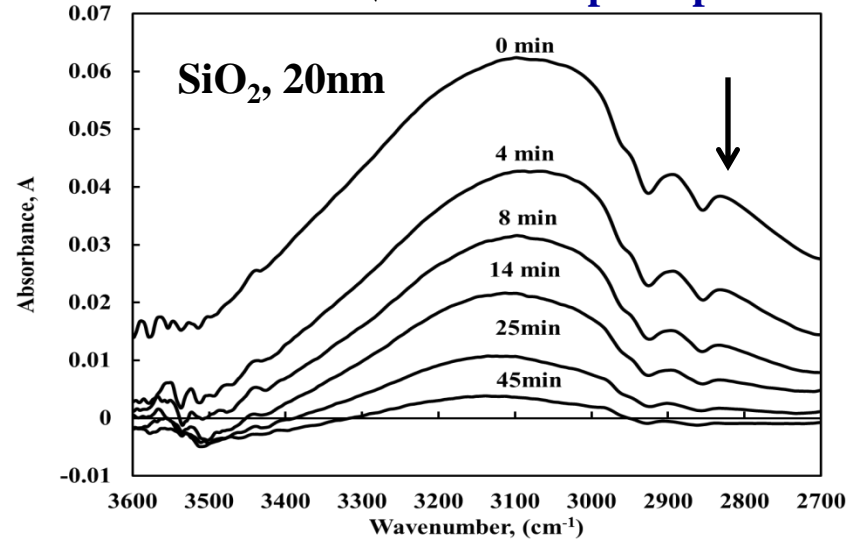
Due to hydrogen bonding, the liquid water stretch vibration is shifted to a lower frequency. Wave number:  $3200\text{ cm}^{-1}$

The main stretching band of water vapor. Wave number:  $3800\text{ cm}^{-1}$

Eliminate the effect of gas phase



Desorption process



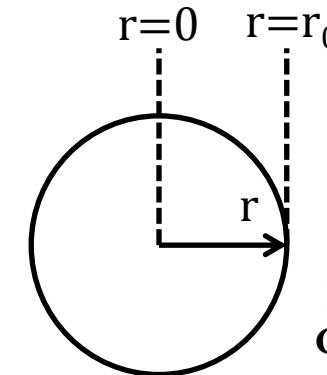
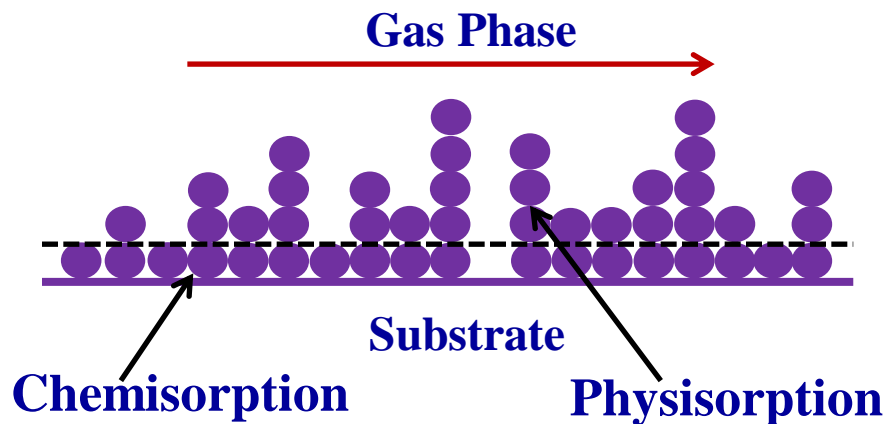
# Process Simulation: Single-Particle Domain

**Adsorbent concentration in the gas phase:**

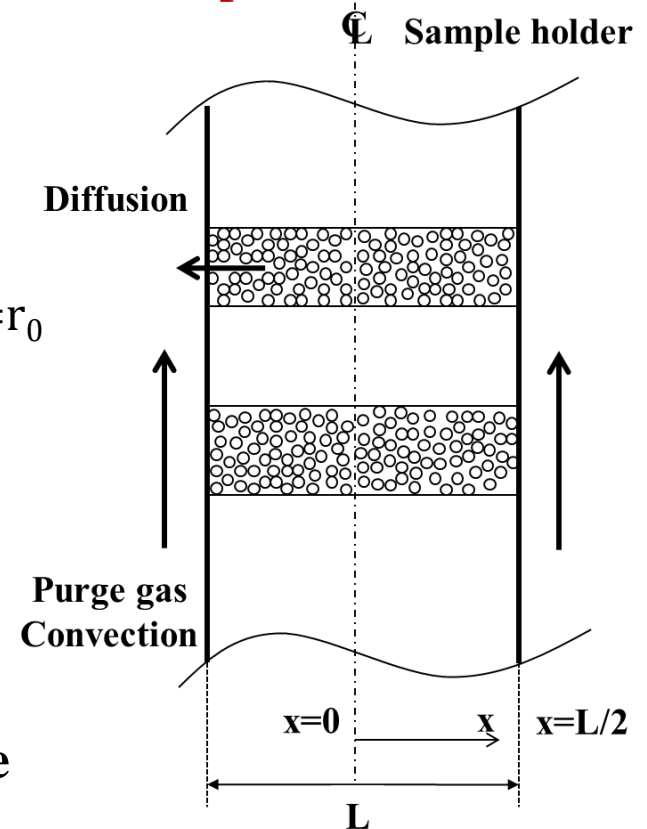
$$\frac{\partial C_{g_{in}}}{\partial t} = \underbrace{D_{e_{in}} \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \frac{\partial C_{g_{in}}}{\partial r} \right)}_{\text{Diffusion term}} + \underbrace{[k_d C_{s_{in}} - k_a C_{g_{in}} (S_0 - C_{s_{in}})] \frac{A_s}{V}}_{\text{Adsorption and desorption term}}$$

**Adsorbent concentration on the surface:**

$$\frac{\partial C_{s_{in}}}{\partial t} = k_a C_{g_{in}} (S_0 - C_{s_{in}}) - k_d C_{s_{in}}$$



**Nanoparticle**

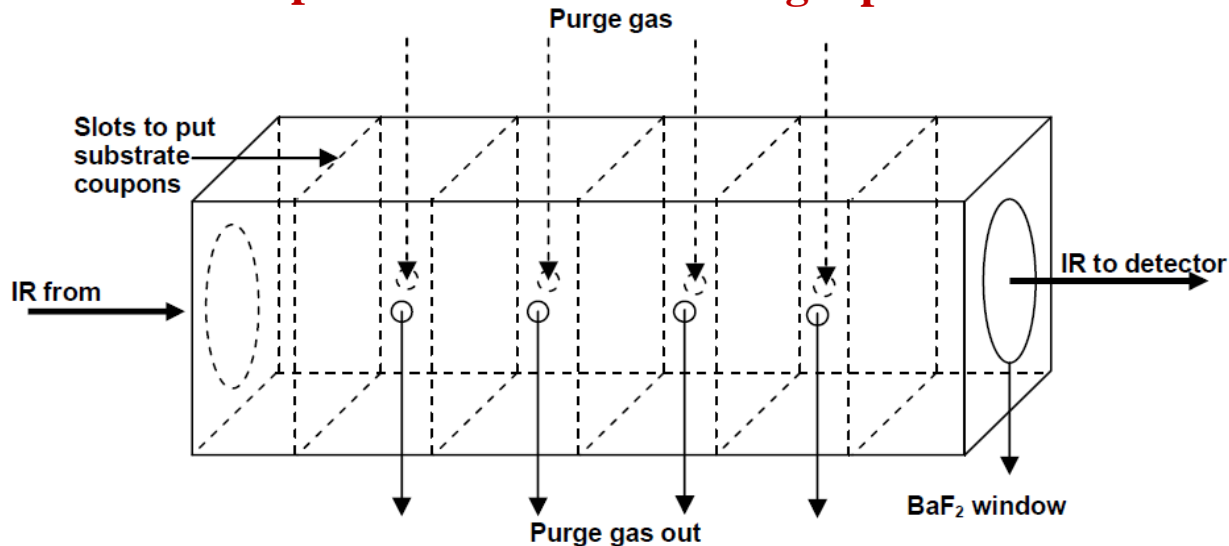


# Process Simulation: Packed-bed Domain

Adsorbent concentration in the gas phase:

$$\frac{\partial C_{gout}}{\partial t} = \underbrace{D_{eout} \frac{\partial^2 C_{gout}}{\partial x^2}}_{\text{Diffusion term in packed-bed domain}} - \underbrace{D_{ein} \frac{\partial C_{gin}}{\partial r} \Big|_{r=r_0} 4\pi r_0^2 N_v}_{\text{Diffusion flux from single-particle domain}}$$

**Diffusion term in packed-bed domain**      **Diffusion flux from single-particle domain**



Integral of absorbance peak over wavenumber:

$$A_{\text{int}} = \int_{\lambda_1}^{\lambda_2} A d\lambda = \frac{a}{r_0} \int_{\lambda_1}^{\lambda_2} a d\lambda \int_0^L \int_0^{r_0} C_{sin}(r, x, t) dr dx.$$



# Mechanism of Multilayer Model

## Adsorption rate coefficients

$$k_a = k_{a_0} \exp\left(\frac{-E_a}{RT}\right)$$

## Desorption rate coefficients

$$k_d = k_{d_0} \exp\left(\frac{-E_d}{RT}\right)$$

## Adsorption activation energies

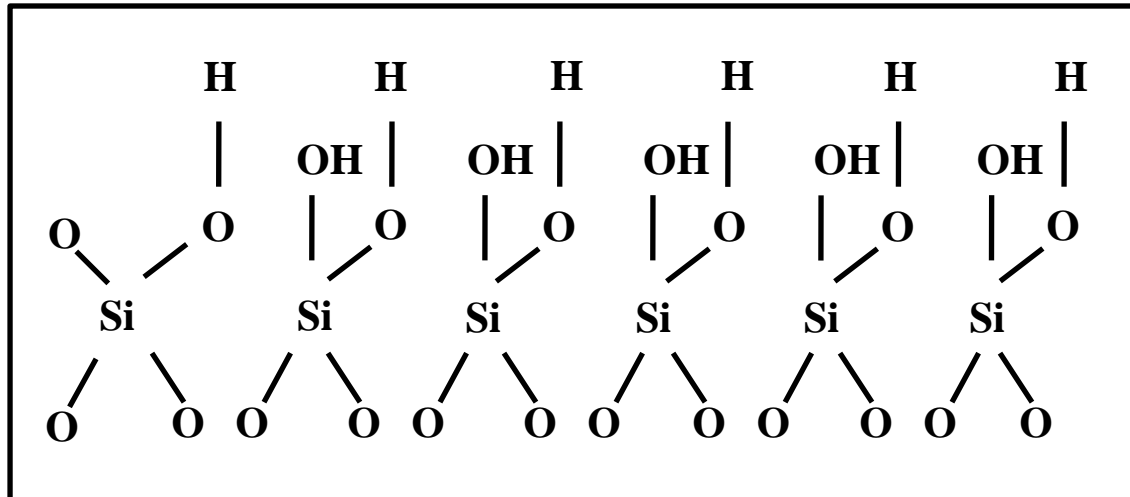
$$E_a = E_{a_1} \frac{C_{s_0} - C_s}{C_{s_0}} + E_{a_2} \frac{C_s}{C_{s_0}}$$

## Desorption activation energies

$$E_d = E_{d_1} \frac{C_{s_0} - C_s}{C_{s_0}} + E_{d_2} \frac{C_s}{C_{s_0}},$$

### 1: Chemisorption

### 2: Physisorption



# Numerical Method

## Discretization

- Forward Euler Method
- Crank-Nicolson Method

## Linearization

- Next Time-step Estimation
- Triangular Matrix Solver

## Iteration

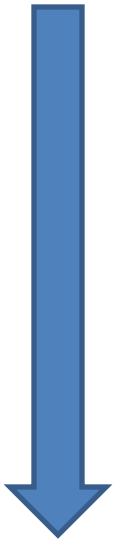
- Update the new value for  $C_{s,in}$
- Update new value for  $k_a, k_d$  and so on



$$\frac{\partial C_g}{\partial t} = \frac{C_{g,i}^{m+1} - C_{g,i}^m}{\Delta t}$$

$$\frac{\partial^2 C_g}{\partial x^2} = \frac{1}{2} \left( \frac{C_{g,i+1}^{m+1} - 2C_{g,i}^{m+1} + C_{g,i-1}^{m+1}}{\Delta x^2} + \frac{C_{g,i+1}^m - 2C_{g,i}^m + C_{g,i-1}^m}{\Delta x^2} \right)$$

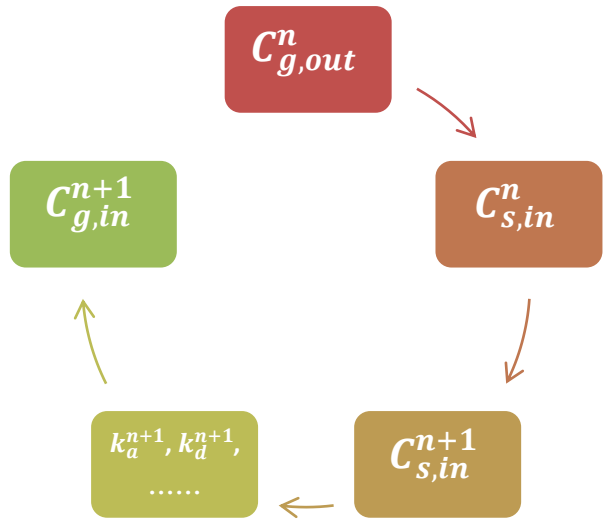
$$C_g = \frac{1}{2} (C_{g,i}^{m+1} + C_{g,i}^m), C_s = C_{s,i}^m.$$



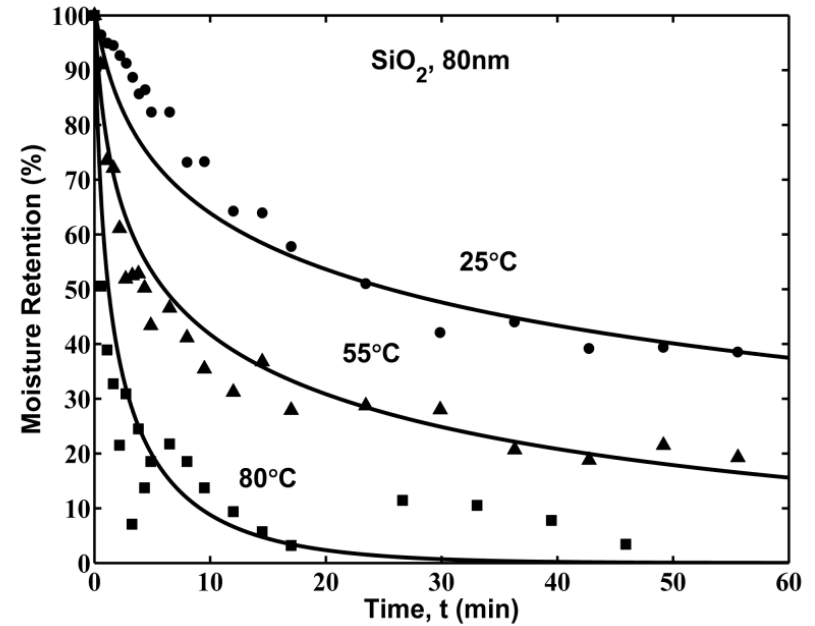
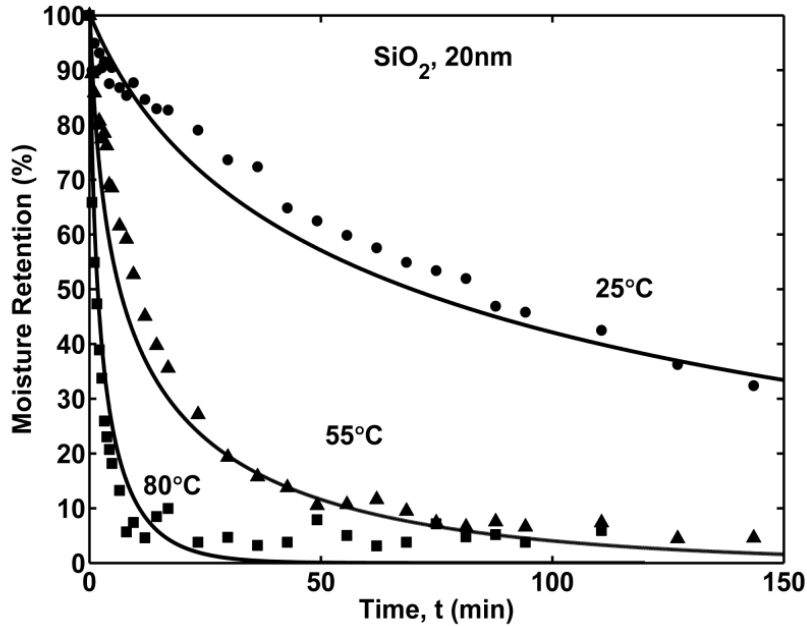
$$\frac{\alpha \Delta \bar{t}}{2 \Delta \bar{x}^2} \bar{C}_{g,i+1}^{m+1} + \left[ \frac{1}{2} (\delta \bar{C}_{s,i}^m - \gamma) \Delta \bar{t} - \frac{\alpha \Delta \bar{t}}{\Delta \bar{x}^2} - 1 \right] \bar{C}_{g,i}^{m+1} + \frac{\alpha \Delta \bar{t}}{2 \Delta \bar{x}^2} \bar{C}_{g,i-1}^{m+1}$$

$$= -\frac{\alpha \Delta \bar{t}}{2 \Delta \bar{x}^2} \bar{C}_{g,i+1}^m + \left[ -\frac{1}{2} (\delta \bar{C}_{s,i}^m - \gamma) \Delta \bar{t} + \frac{\alpha \Delta \bar{t}}{\Delta \bar{x}^2} - 1 \right] \bar{C}_{g,i}^m$$

$$- \frac{\alpha \Delta \bar{t}}{2 \Delta \bar{x}^2} \bar{C}_{g,i-1}^m - \Delta \bar{t} \beta \bar{C}_{s,i}^m$$

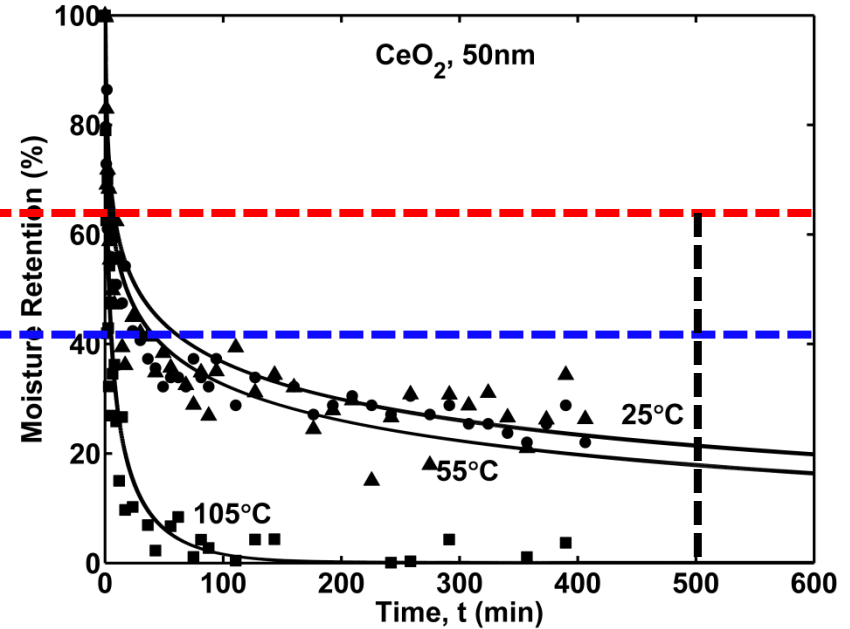
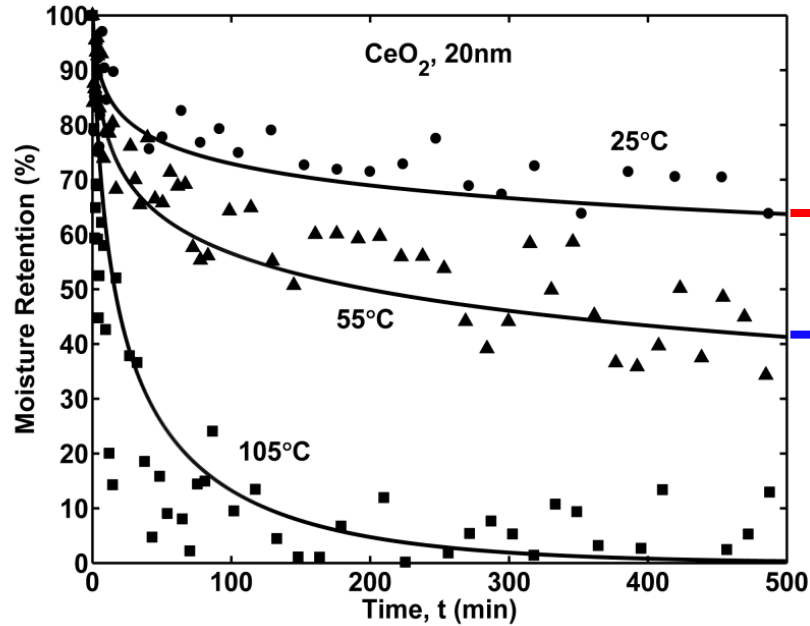


# Comparison of Adsorption Profiles of NPs (I)



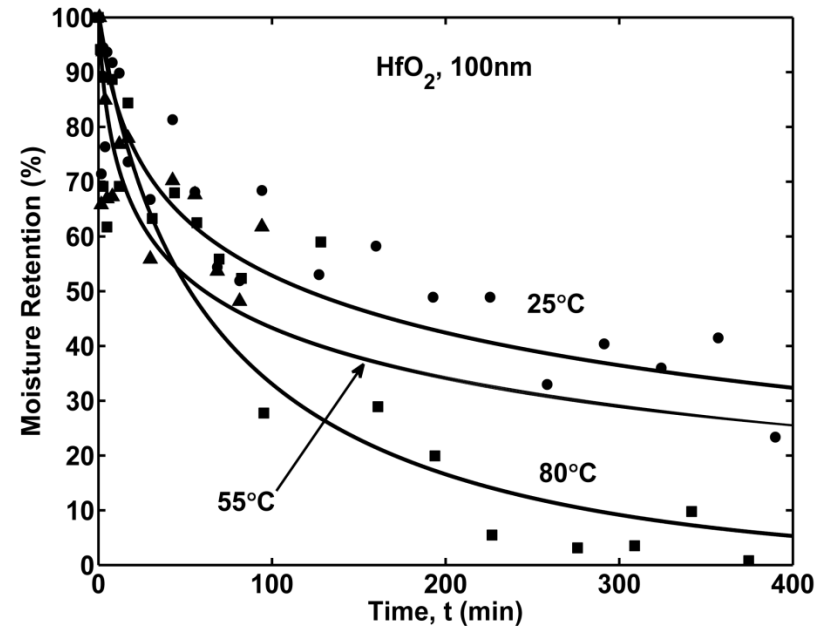
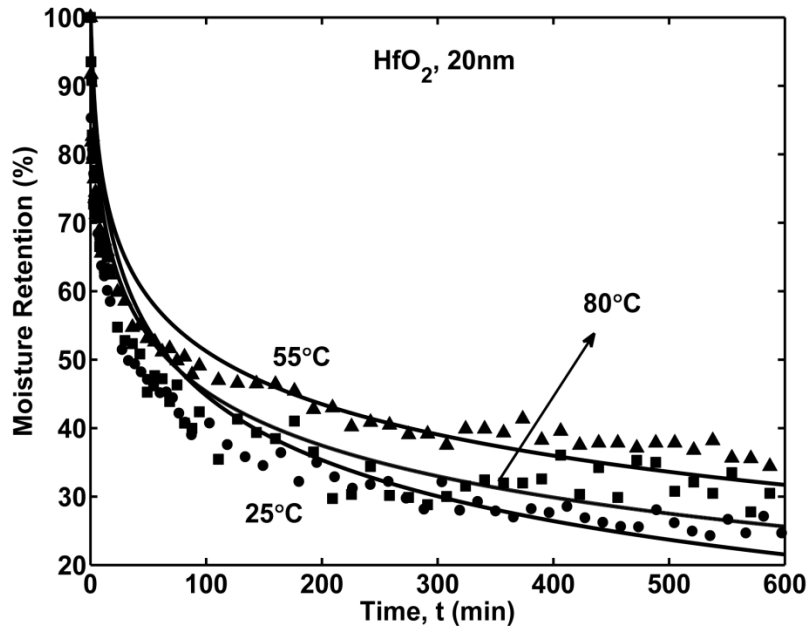
Sample	Saturated surface concentration $C_{S0}$ (gmol m <sup>-2</sup> )	Fractional coverage $\theta$ (%)	$E_{a1}$ (kJ gmol <sup>-1</sup> )	$E_{a2}$ (kJ gmol <sup>-1</sup> )	$E_{d1}$ (kJ gmol <sup>-1</sup> )	$E_{d2}$ (kJ gmol <sup>-1</sup> )
SiO <sub>2</sub> (20 nm), 25°C	$2.0 \times 10^{-6}$	67	9.0	6.0	16.0	12.5
SiO <sub>2</sub> (20 nm), 55°C	$1.9 \times 10^{-6}$	63	9.0	1.2	13.0	8.0
SiO <sub>2</sub> (20 nm), 80°C	$1.5 \times 10^{-6}$	50	9.0	0.1	7.6	5.7
SiO <sub>2</sub> (80 nm), 25°C	$1.1 \times 10^{-6}$	37	10.0	6.5	15.5	10.0
SiO <sub>2</sub> (80 nm), 55°C	$1.0 \times 10^{-6}$	33	10.0	2.0	12.5	5.5
SiO <sub>2</sub> (80 nm), 80°C	$5.3 \times 10^{-7}$	18	10.0	1.0	7.5	2.2

# Comparison of Adsorption Profiles of NPs (II)



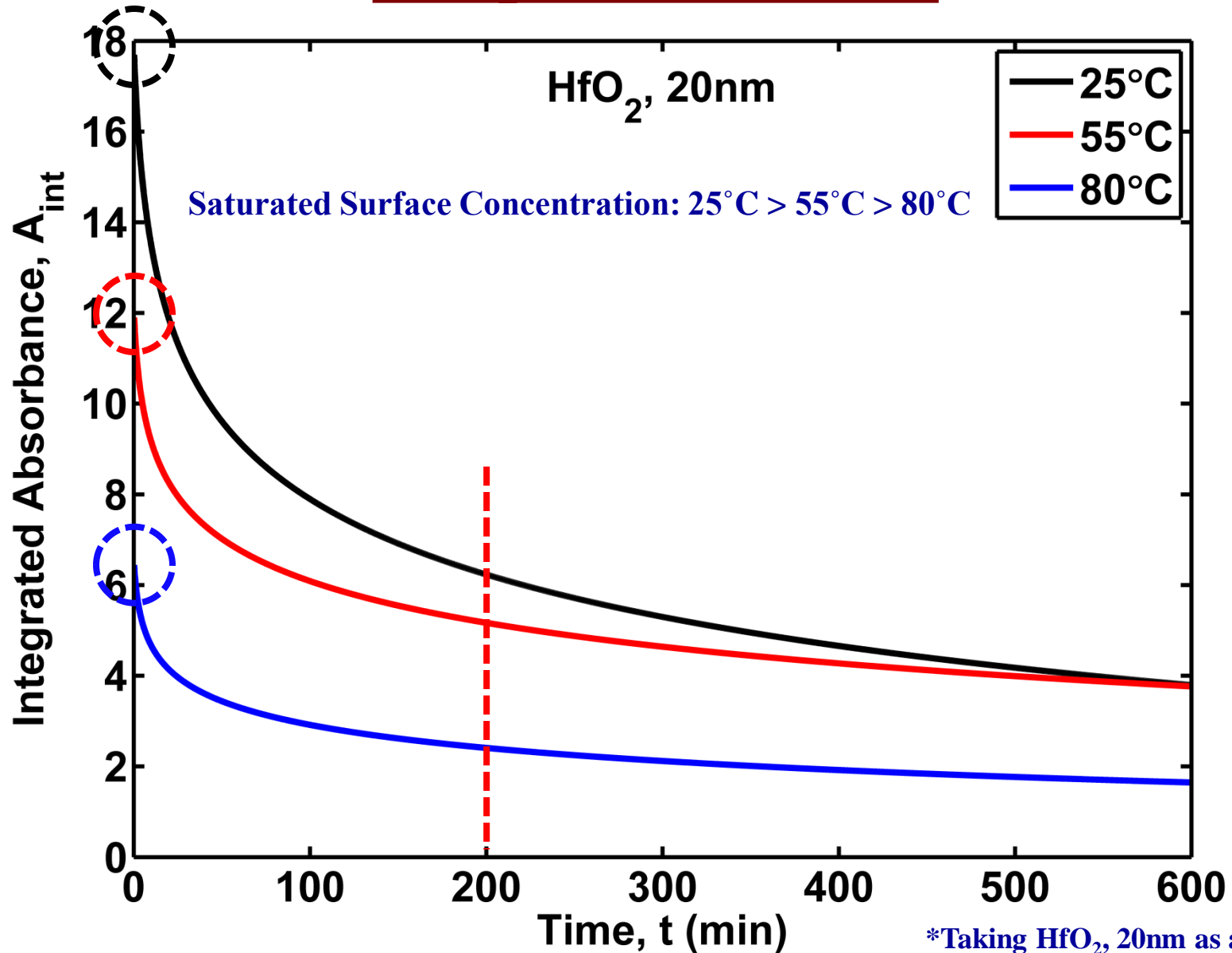
Sample	Saturated surface concentration $C_{S_0}$ (gmol m <sup>-2</sup> )	Fractional coverage $\theta$ (%)	$E_{a1}$ (kJ gmol <sup>-1</sup> )	$E_{a2}$ (kJ gmol <sup>-1</sup> )	$E_{d1}$ (kJ gmol <sup>-1</sup> )	$E_{d2}$ (kJ gmol <sup>-1</sup> )
CeO <sub>2</sub> (20 nm), 25°C	$8.3 \times 10^{-7}$	10.4	1.9	1.5	46	7.8
CeO <sub>2</sub> (20 nm), 55°C	$8.2 \times 10^{-7}$	10.3	1.9	1.2	30	8.1
CeO <sub>2</sub> (20 nm), 105°C	$8.1 \times 10^{-7}$	10.1	1.9	1.0	10	8.9
CeO <sub>2</sub> (50 nm), 25°C	$5.5 \times 10^{-7}$	6.9	3.0	0.1	19	5.3
CeO <sub>2</sub> (50 nm), 55°C	$3.7 \times 10^{-7}$	4.6	3.0	0.1	20	4.7
CeO <sub>2</sub> (50 nm), 105°C	$3.6 \times 10^{-8}$	4.5	3.0	0.1	9	5.0

# Comparison of Adsorption Profiles of NPs (III)



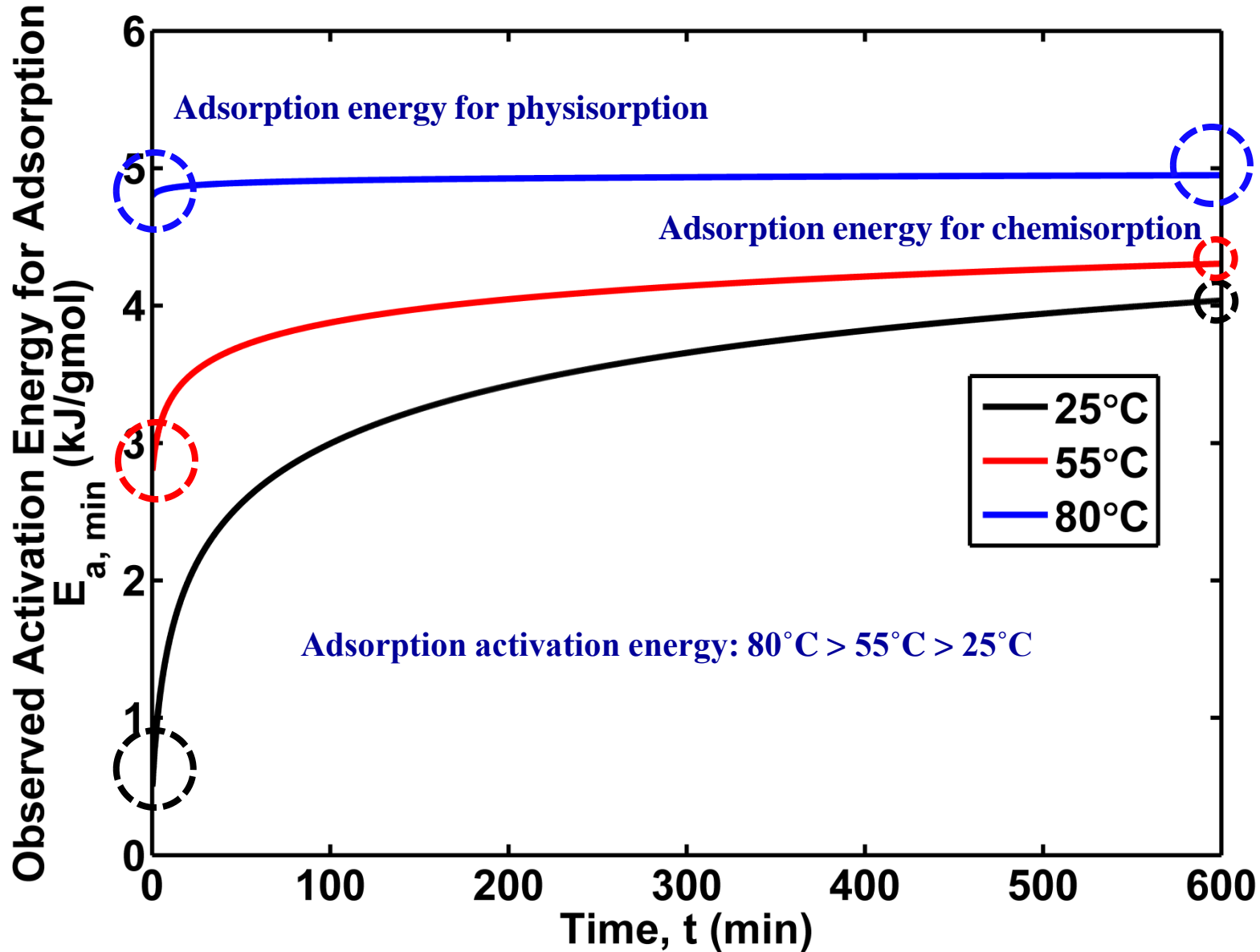
Sample	Saturated surface concentration $C_{S_0}$ (gmol m <sup>-2</sup> )	Fractional coverage $\theta$ (%)	$E_{a1}$ (kJ gmol <sup>-1</sup> )	$E_{a2}$ (kJ gmol <sup>-1</sup> )	$E_{d1}$ (kJ gmol <sup>-1</sup> )	$E_{d2}$ (kJ gmol <sup>-1</sup> )
HfO <sub>2</sub> (20 nm), 25°C	$2.2 \times 10^{-6}$	55	5.0	0.5	17.0	0.4
HfO <sub>2</sub> (20 nm), 55°C	$1.5 \times 10^{-6}$	38	5.0	2.8	23.5	0.7
HfO <sub>2</sub> (20 nm), 80°C	$8.1 \times 10^{-7}$	20	5.0	4.8	22.0	0.016
HfO <sub>2</sub> (100 nm), 25°C	$4.4 \times 10^{-7}$	11	12.5	10.5	16.5	4.6
HfO <sub>2</sub> (100 nm), 55°C	$3.3 \times 10^{-7}$	8.3	12.5	11.0	16.0	3.7
HfO <sub>2</sub> (100 nm), 80°C	$3.1 \times 10^{-7}$	7.8	12.5	12.0	11.0	2.6

# Temperature Effect

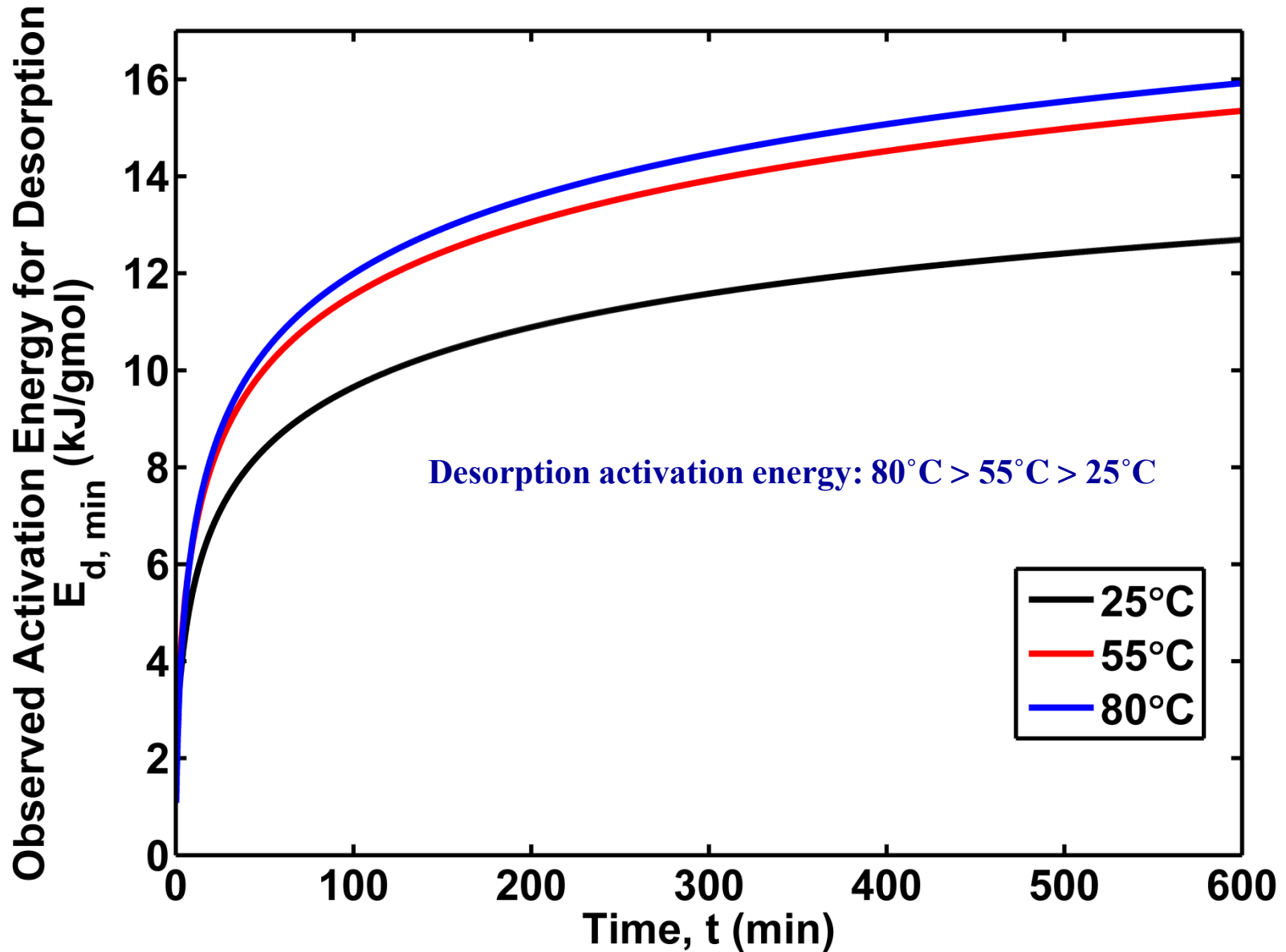


\*Taking HfO<sub>2</sub>, 20nm as an example

# Temperature Effect

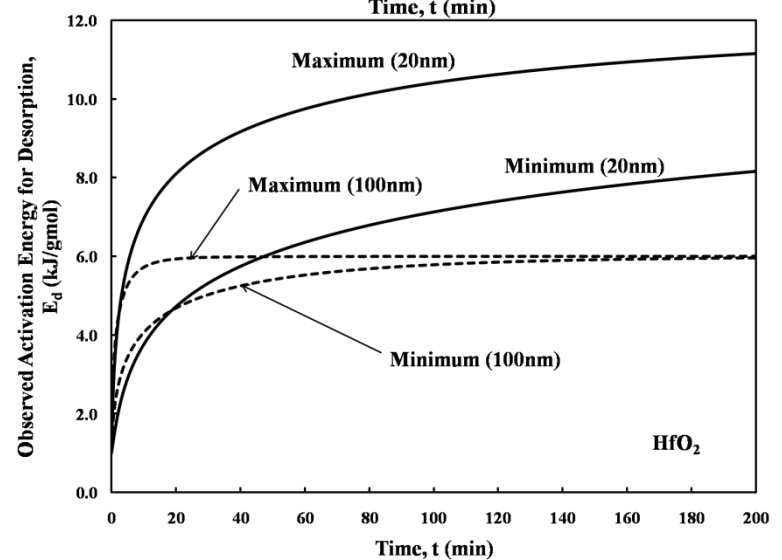
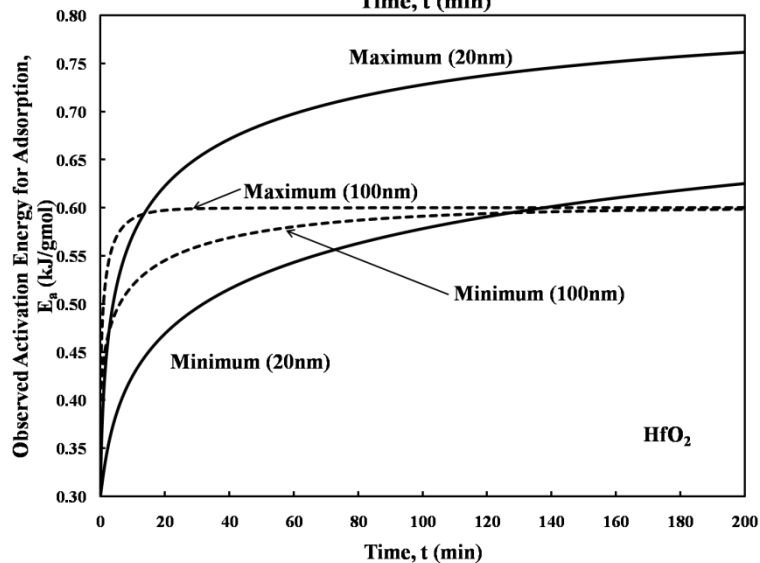
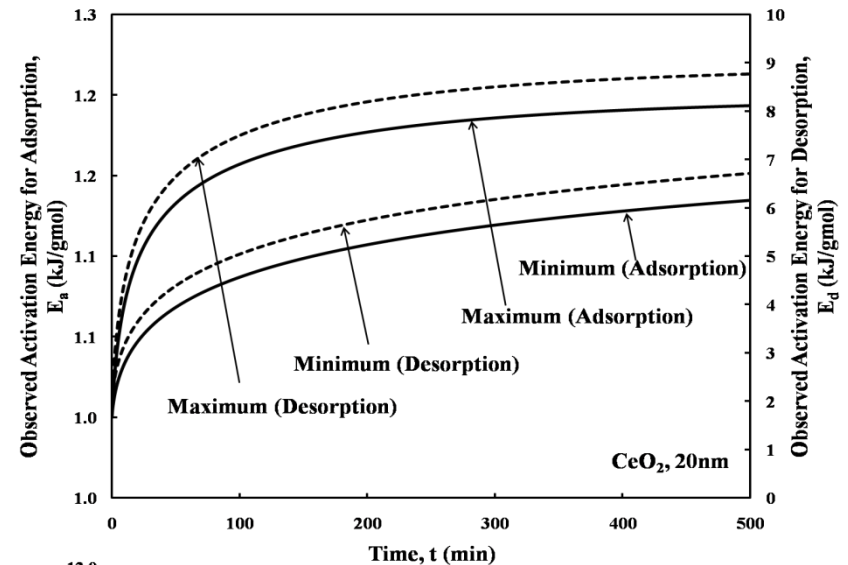
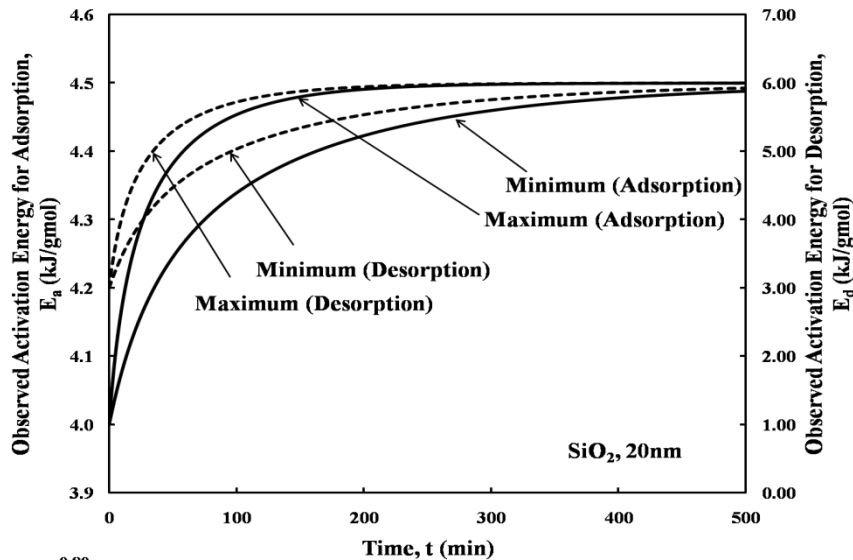


# Temperature Effect

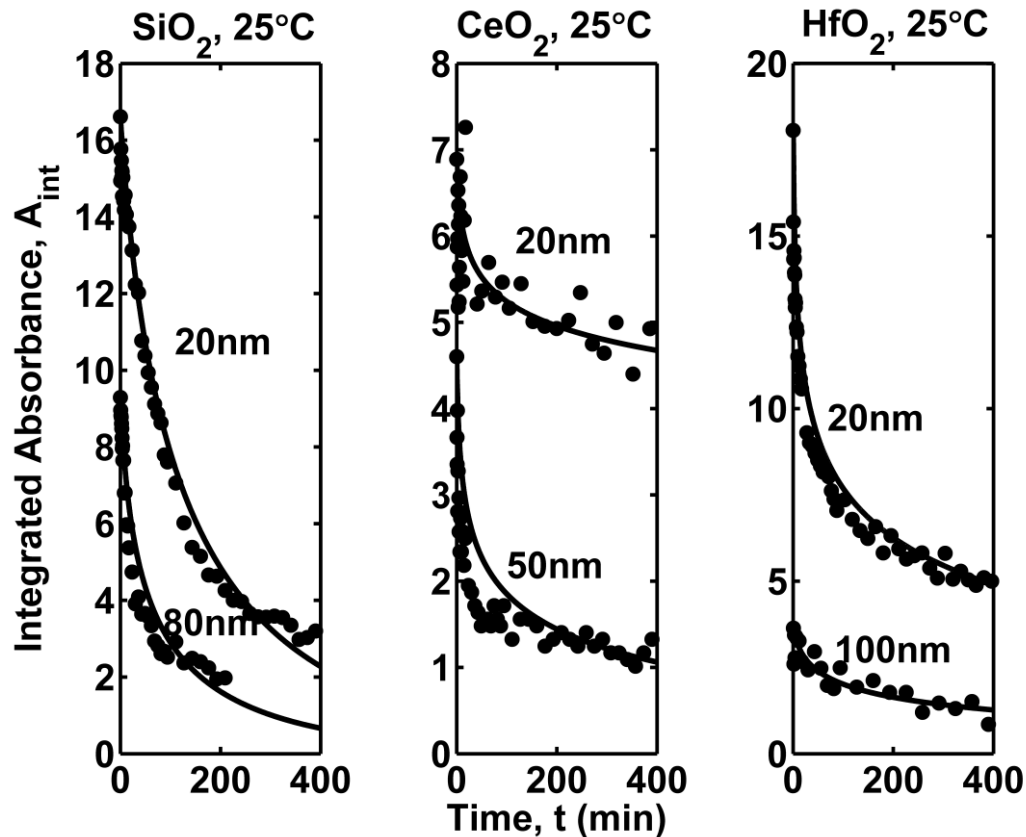




# Activation Energy of Surface Processes

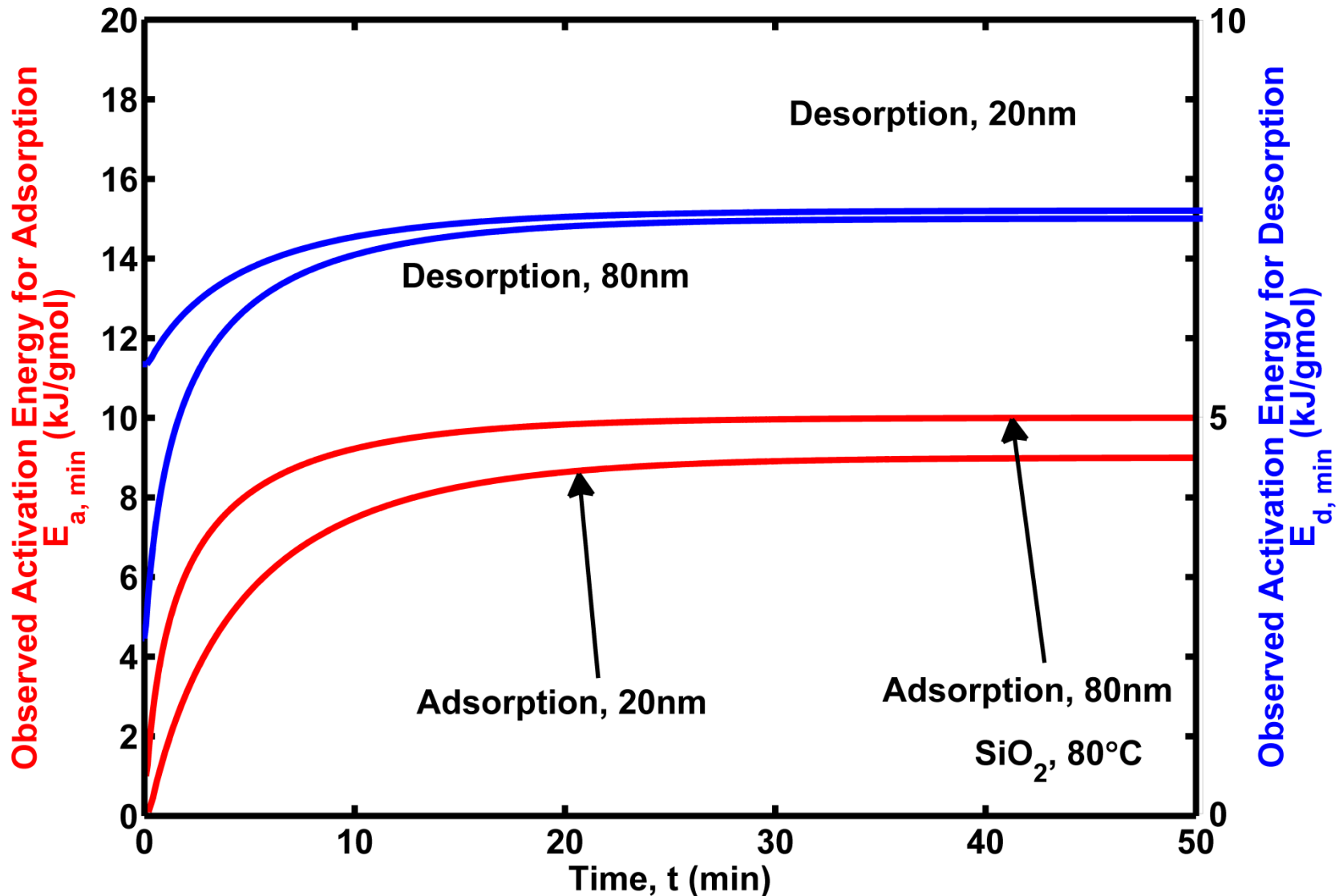


# Size Effect on NP Surface Properties

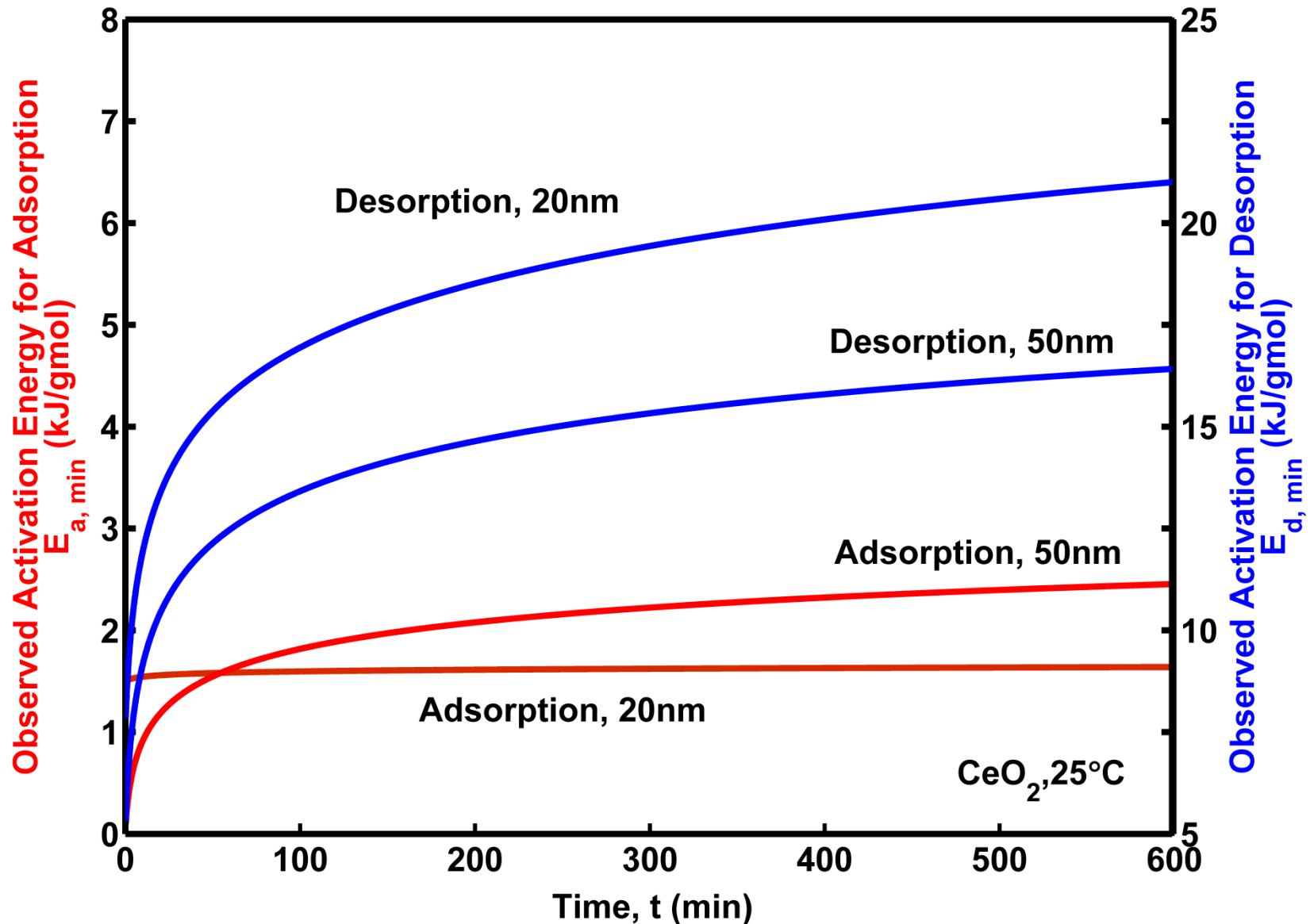


- The surface retention characteristics depend on the particle size.
- Nanoparticles with smaller size will have larger density of surface sites and larger surface retention capacity. They also have higher affinity for retention of contaminants.

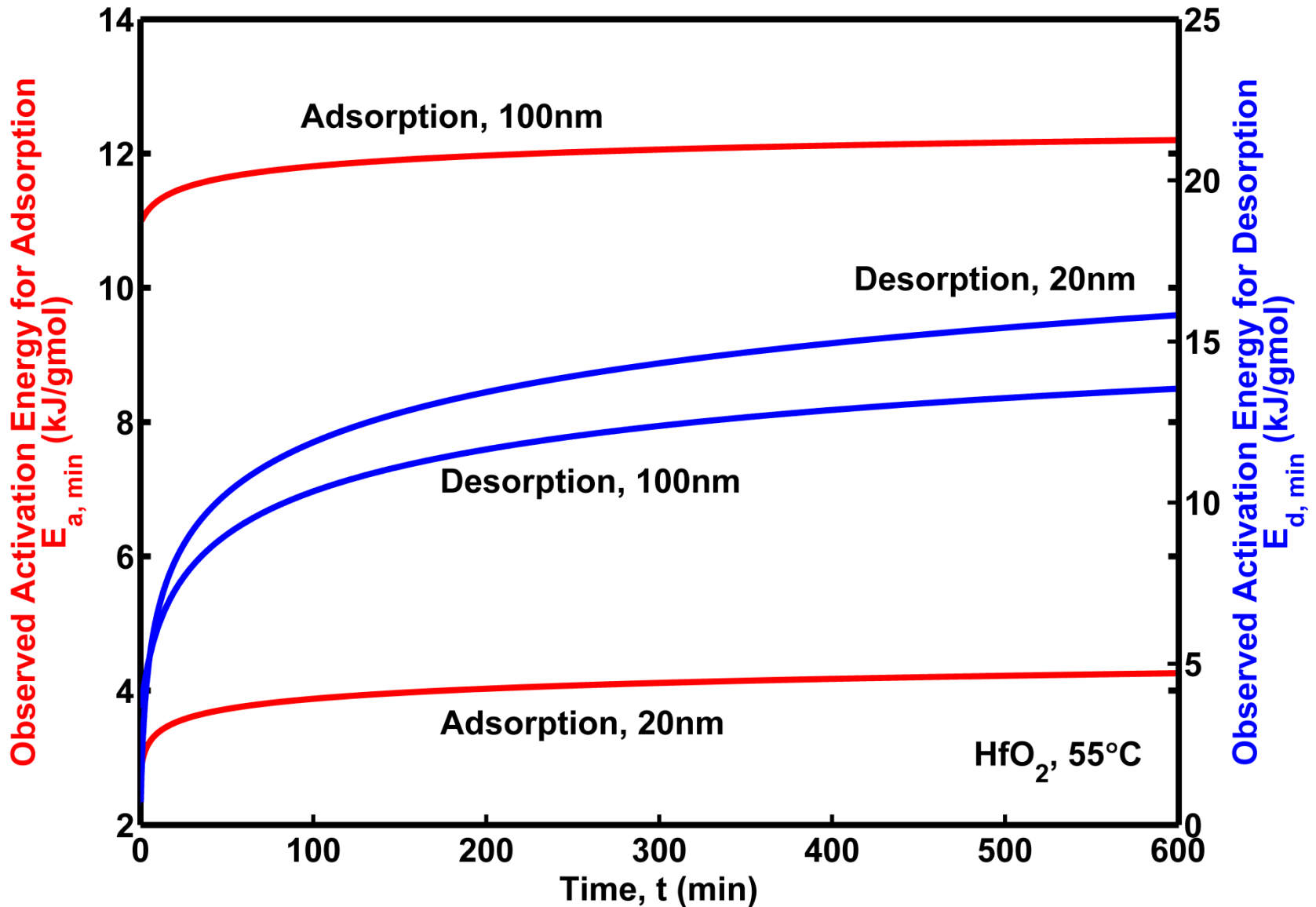
# Size Effect on Energy of Surface Processes



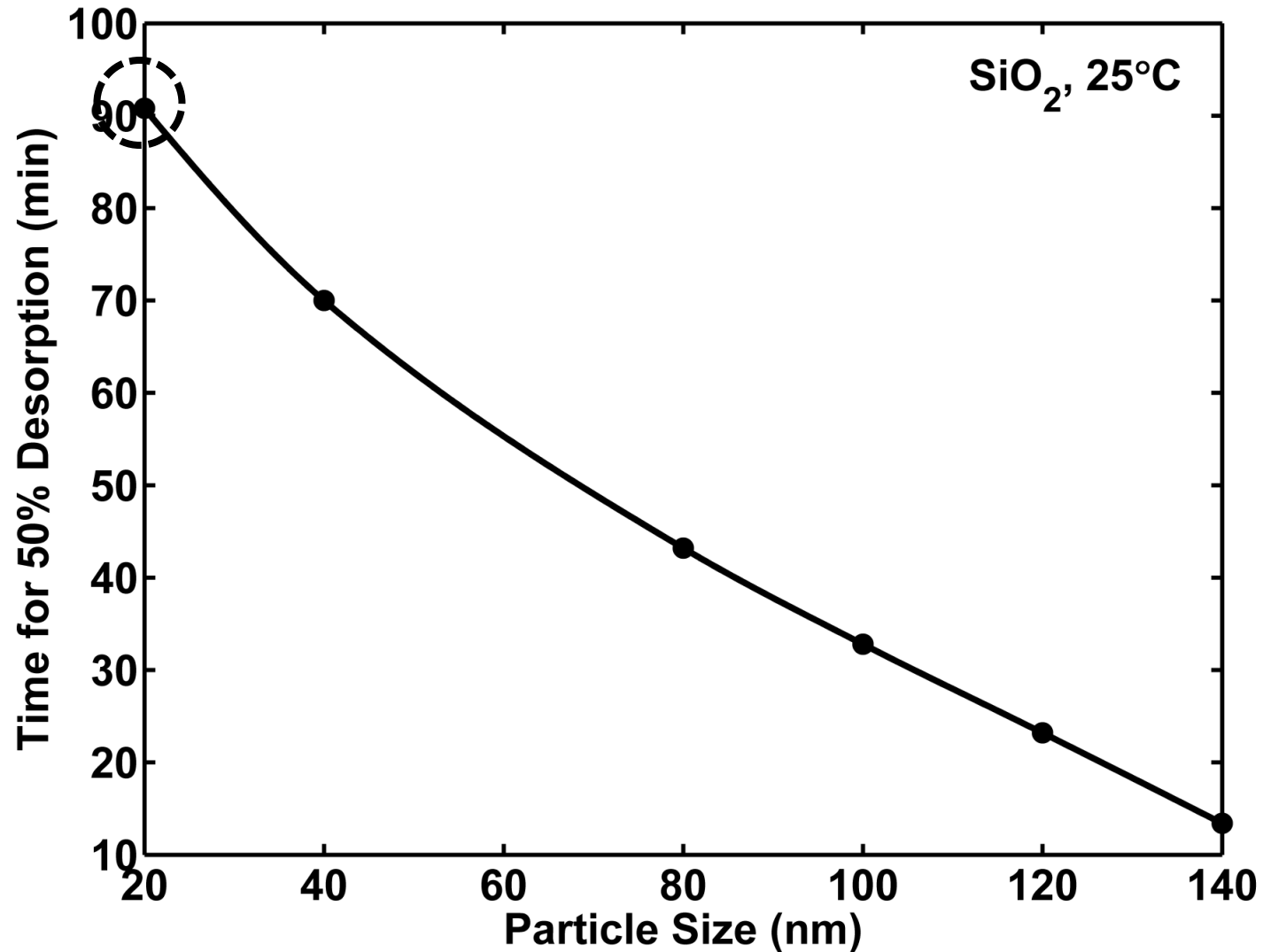
# Size Effect on Energy of Surface Processes



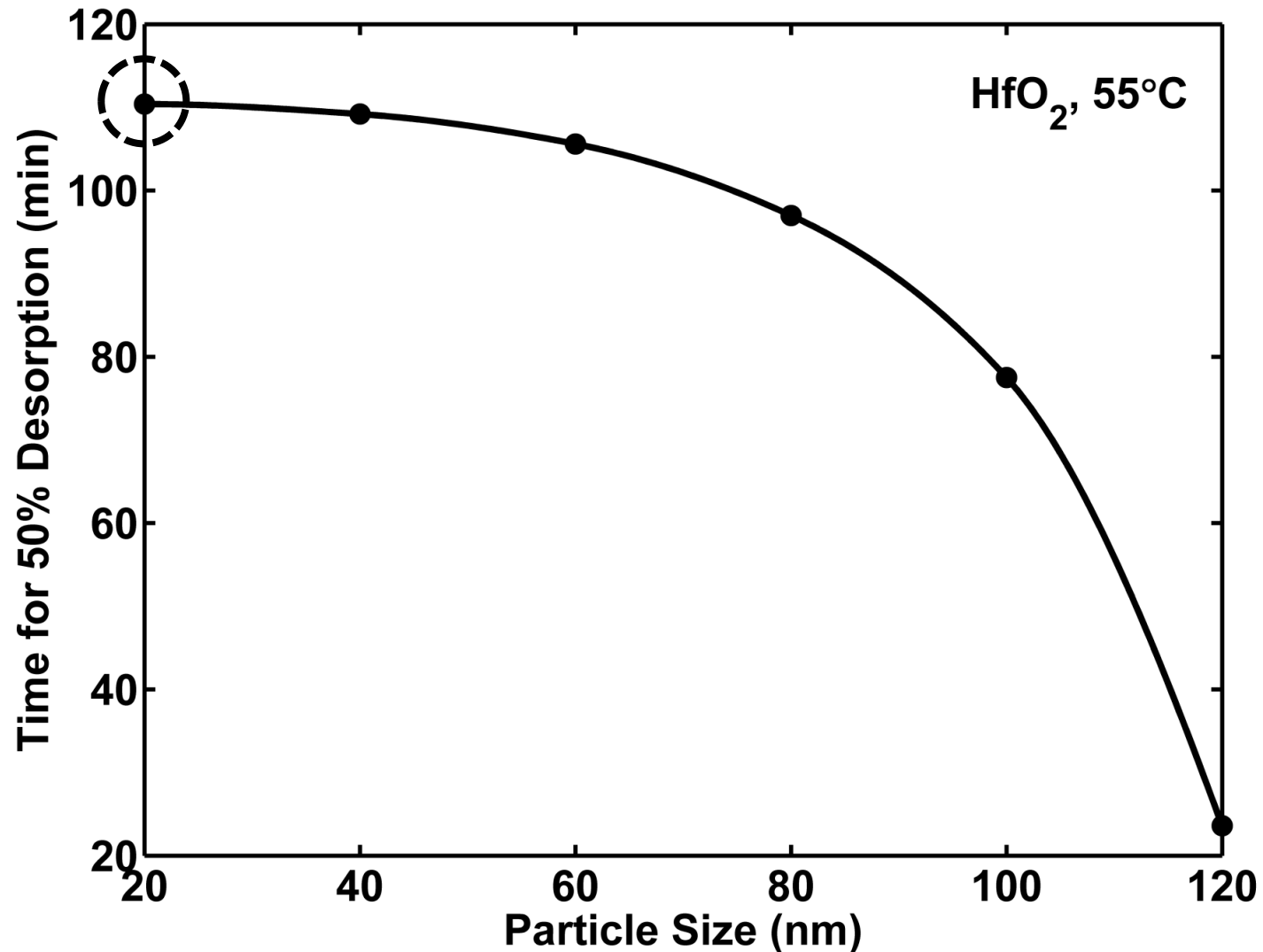
# Size Effect on Energy of Surface Processes



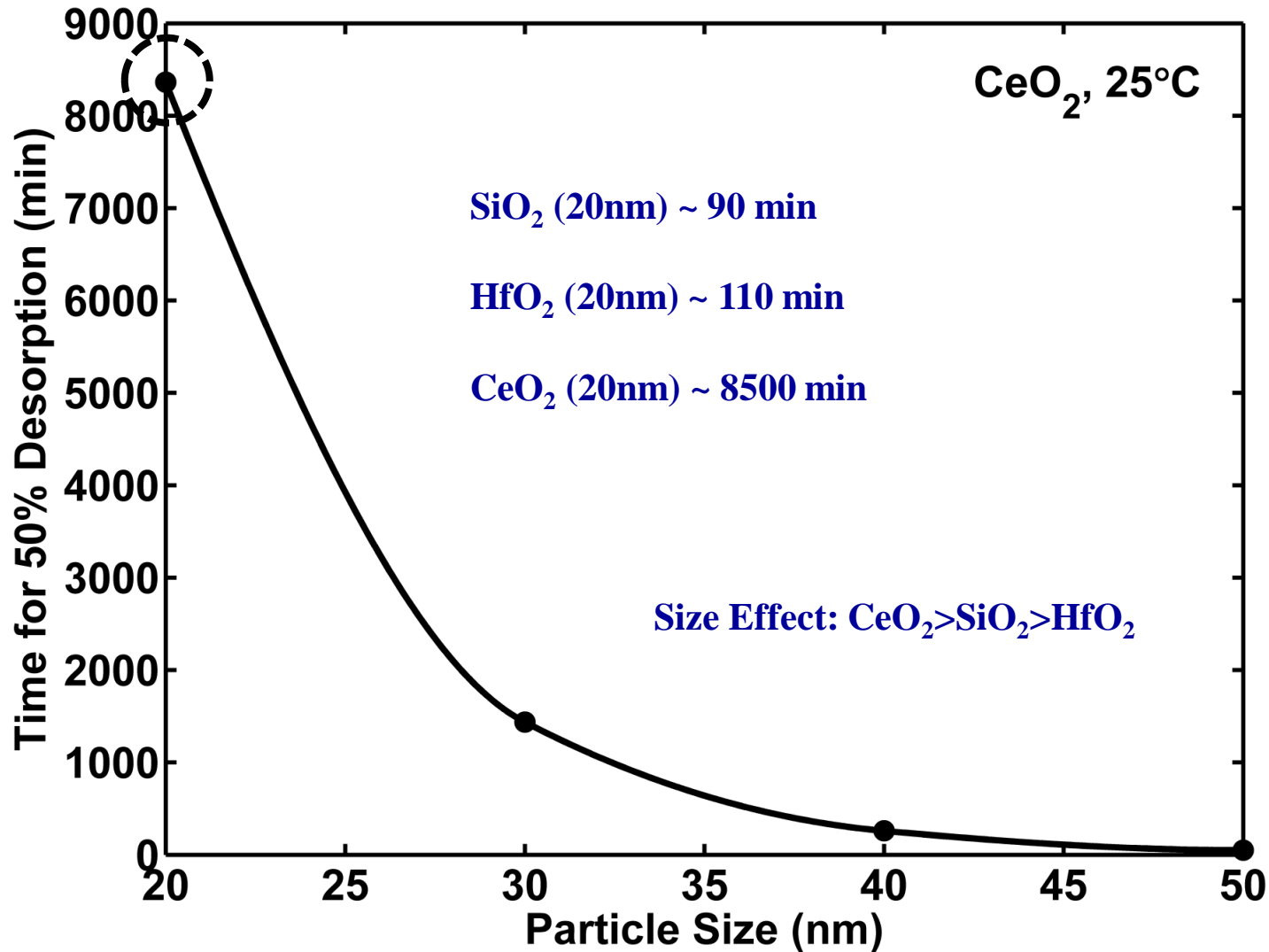
# Model Prediction on Desorption Time



# Model Prediction on Desorption Time



# Model Prediction on Desorption Time





# Dimensionless Single NP Model

## Dimensionless forms:

$$\bar{C}_{gin} = \frac{C_{gin}}{C_{gin,0}}, \quad \bar{C}_{sin} = \frac{C_{sin}}{C_{sin,0}}, \quad \bar{r} = \frac{r}{r_0}, \quad \bar{t} = \frac{t}{\frac{V}{A_0 k_a S_0}}, \quad \bar{k}_a = \frac{k_a}{k_{ac}}, \quad \bar{k}_d = \frac{k_d}{k_{dc}}$$

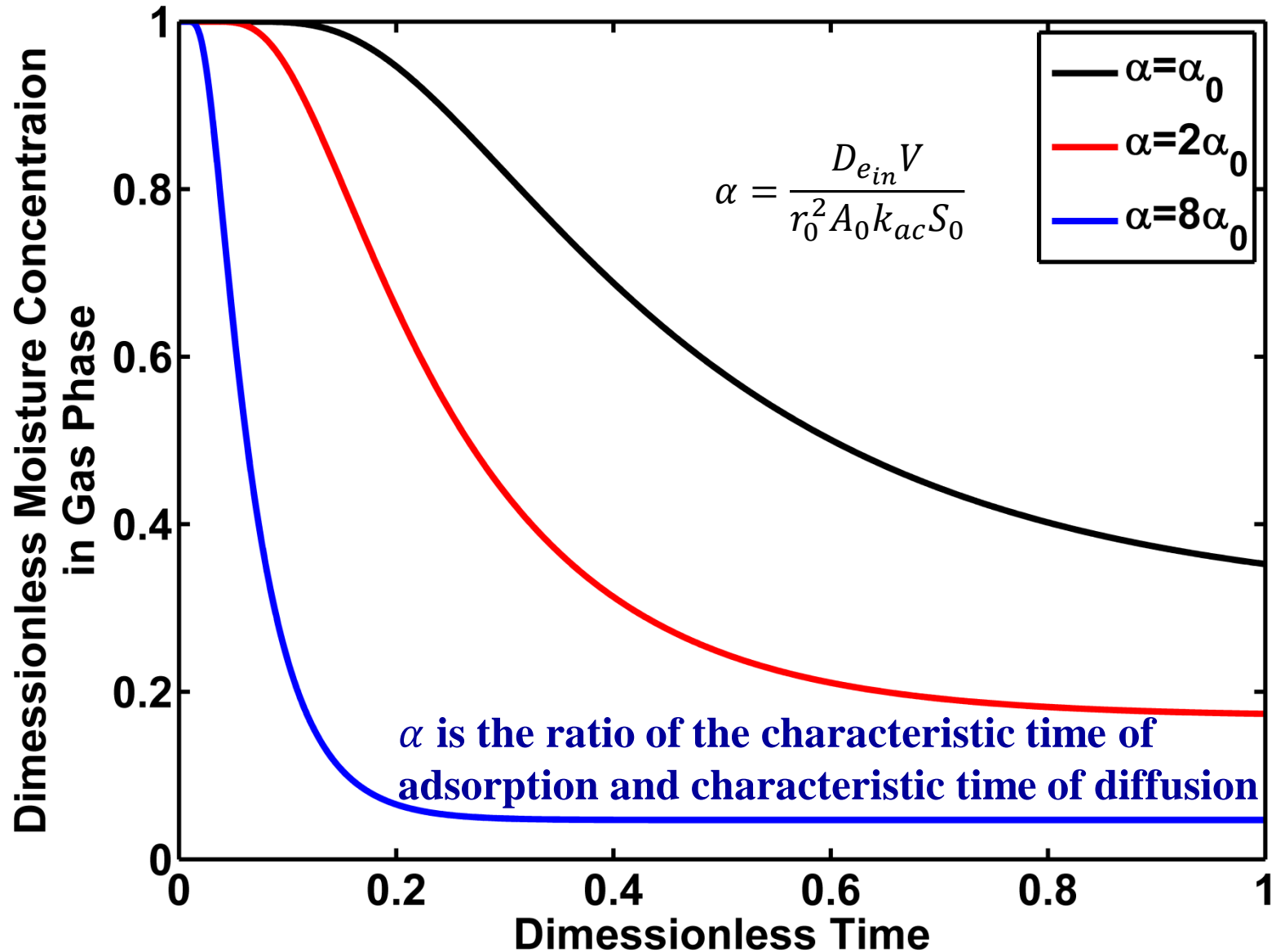
## Dimensionless governing equations:

$$\frac{\partial \bar{C}_{gin}}{\partial \bar{t}} = \frac{D_{ein} V}{r_0^2 A_0 k_{ac} S_0} \frac{1}{\bar{r}^2} \frac{\partial}{\partial \bar{r}} \left( \bar{r}^2 \frac{\partial \bar{C}_{gin}}{\partial \bar{r}} \right) + \frac{C_{sin,0} k_{dc}}{C_{gin,0} k_{ac} S_0} \bar{C}_{sin} \bar{k}_d - \bar{k}_a \bar{C}_{gin} + \frac{C_{sin,0}}{S_0} \bar{k}_a \bar{C}_{gin} \bar{C}_{sin}$$
$$\frac{\partial \bar{C}_{sin}}{\partial \bar{t}} = \frac{C_{gin,0} V}{C_{sin,0} A_0} \bar{k}_a \bar{C}_{gin} - \frac{C_{gin,0} V}{A_0 S_0} \bar{k}_a \bar{C}_{gin} \bar{C}_{sin} - \frac{k_{dc} V}{k_{ac} A_0 S_0} \bar{k}_d \bar{C}_{sin}$$

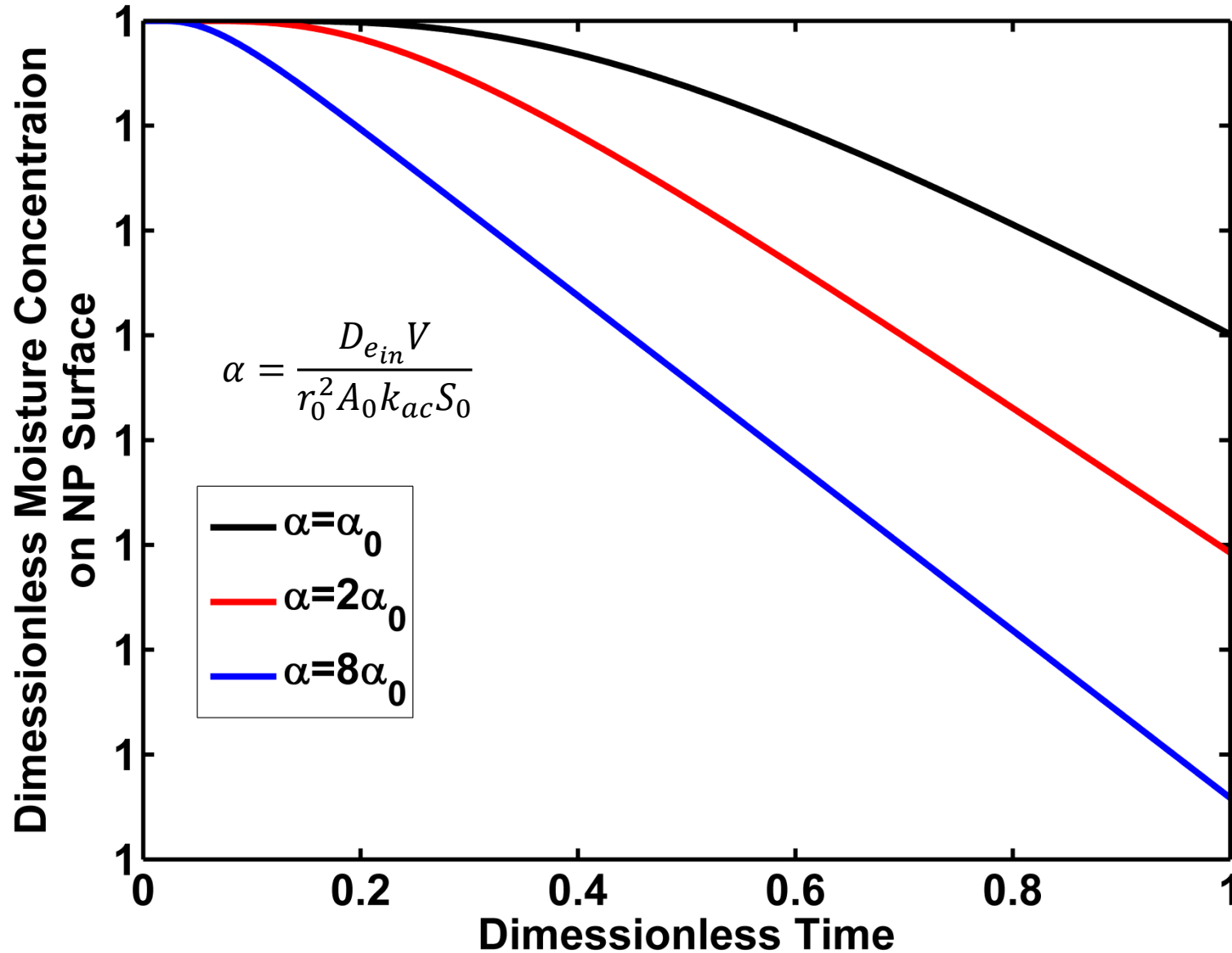
## Dimensionless groups:

$$\alpha = \frac{D_{ein} V}{r_0^2 A_0 k_{ac} S_0}, \quad \beta = \frac{C_{sin,0} k_{dc}}{C_{gin,0} k_{ac} S_0}, \quad \gamma = \frac{C_{sin,0}}{S_0},$$
$$\eta = \frac{C_{gin,0} V}{C_{sin,0} A_0}, \quad \theta = \frac{C_{gin,0} V}{A_0 S_0}, \quad \omega = \frac{k_{dc} V}{k_{ac} A_0 S_0},$$

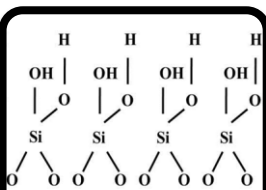
# Parametric Study



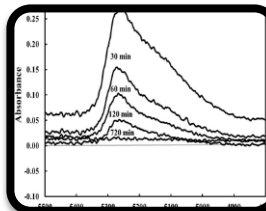
# Parametric Study



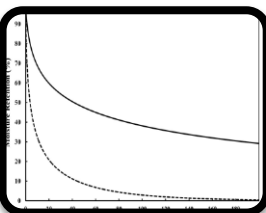
# Summary and Conclusions



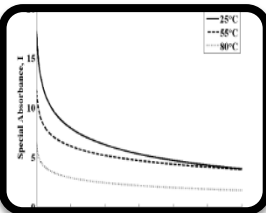
**Hydroxylation is a powerful method for characterization of capture and retention (adsorption/desorption) properties of NPs.**



**The surface retention characteristics depend on the material as well as on the particle size and temperature.**



**NPs with smaller size will have larger density of surface sites and larger surface retention. They also have higher affinity for retention of contaminants. Based on the size effect on energy, smaller NPs would have higher desorption activation energy and lower adsorption activation energy.**



**Purge under the higher temperature would benefit the desorption of moisture on the NP surface.**

# Future Work

Keep on studying  
the surface  
properties of other  
NPs

Parametric study  
based on the  
dimensionless single  
NP model

Upgrade the  
numerical model  
and increase the  
efficiency

# Publications and Presentations

- Hao Wang, F. Shadman, Effect of Particle Size on the Adsorption and Desorption Properties of Oxide Nanoparticles, Submitted to AIChE, April, 2012
- Hao Wang, J. Yao, F. Shadman, Characterization of the Surface Properties of Nanoparticles Using Moisture Adsorption Dynamic Profiling, Chemical Engineering Science, June 2011
- Hao Wang, Characterization of the Surface Properties of Nanoparticles Using Moisture Adsorption Dynamic Profiling, SRC/SEMATECH Teleconference, July 2011 [PRESENTATION]
- Hao Wang, Physicochemical and Surface Characteristics Study of Nanoparticles related to ESH Impact of Emerging Nanoparticles and Byproduct in Semiconductor Manufacturing, SRC/SEMATECH Teleconference, November 2010 [PRESENTATION]

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- Farhang Shadman, Professor of Chemical and Environmental Engineering, UA.
- Reyes Sierra, Professor of Chemical & Environmental Engineering, UA.
- Buddy Ratner, Professor of Bioengineering, UW.
- Junpin Yao, Matheson Tri-Gas Inc.